

THE KAVERY ENGINEERING COLLEGE

(An Autonomous Institution)

B.E/B.TECH DEGREE END SEMESTER THEORY EXAMINATIONS, APRIL/MAY 2026

Fourth Semester

Chemical Engineering

UMAT24401 / MA3451 - Transform Techniques

Regulations - 2024 & 2021

Duration : 3 Hrs

Maximum : 100 Marks

PART - A (ANSWER ALL QUESTIONS) (Marks 10*2=20)

Q.No	Questions	BTL	CO	Marks
1.	Prove that $\vec{F} = (y^2 \cos x + z^3)\vec{i} + (2y \sin x - 4)\vec{j} + 3xz^2\vec{k}$ is irrotational.	L2	1	2
2.	State Stoke's theorem.	L1	1	2
3.	Define Dirichlet's conditions.	L1	2	2
4.	Find the Fourier constants b_n for $x \sin x$ in $(-\pi, \pi)$.	L2	2	2
5.	Define Fourier transform Pair.	L1	3	2
6.	If $F_c[e^{-ax}] = \sqrt{\frac{2}{\pi}} \left[\frac{a}{s^2 + a^2} \right]$ find $F_c[x e^{-ax}]$.	L2	3	2
7.	State and prove Initial Value Theorem.	L1	4	2
8.	If $f(t) = e^{-2t} \sin 2t$, find $L[f'(t)]$.	L2	4	2
9.	State the convolution theorem on Z - Transform.	L1	5	2
10.	Find $Z[e^{-at}]$	L2	5	2

PART - B (ANSWER ALL QUESTIONS) (Marks 5*16 = 80)

Q.No	Questions	BLT	CO	Marks
11.	a Verify Gauss divergent theorem for $\vec{F} = x^2\vec{i} + y^2\vec{j} + z^2\vec{k}$ the cube bounded by the planes $x = 0, x = 1, y = 0, y = 1, z = 0, z = 1$.	L4	1	16
	Or			
	b Verify Stoke's theorem for vector field $\vec{F} = xy\vec{i} - 2yz\vec{j} - zx\vec{k}$ where s is the surface of the rectangular parallelepiped formed by $x = 0, y = 0, z = 0, x = 1, y = 2, z = 3$ above the xy -plane.	L4	1	16
12.	a i Determine the Fourier series expansion of $f(x) = x^2$ in $(-\pi, \pi)$ and hence show that $\frac{1}{1^4} + \frac{1}{2^4} + \frac{1}{3^4} + \dots = \frac{\pi^4}{90}$.	L2	2	8
	ii Find the fourier series of period 2π for the function $f(x) = x \cos x$ in $0 < x < 2\pi$.	L3	2	8

Or

- b i Obtain a Fourier expansion for $f(x) = |x|$ in $-\pi \leq x \leq \pi$. L2 2 8
- ii Find the first fundamental harmonic of the Fourier series of $f(x)$ given by the following table. L3 2 8
- | | | | | | | |
|--------|---|----|----|----|----|----|
| x | 0 | 1 | 2 | 3 | 4 | 5 |
| $f(x)$ | 9 | 18 | 24 | 28 | 26 | 20 |

13. a i Find the Fourier transform of $f(x) = e^{-\frac{x^2}{2}}$ in $(-\infty, \infty)$. L3 3 8

- ii Find the Fourier transform of $f(x) = \begin{cases} a^2 - x^2, & |x| < a \\ 0 & |x| > 0 \end{cases}$ Hence prove that L3 3 8

$$\int_0^{\infty} \frac{\sin x - x \cos x}{x^3} dx = \frac{\pi}{4}$$

Or

- b i Evaluate $\int_0^{\infty} \frac{s^2}{(s^2+a^2) + (s^2+b^2)} ds$ using Fourier Transforms. L3 3 8

- ii Find the Fourier transform of the function $f(x) = \begin{cases} 1 - |x|, & |x| \leq 1 \\ 0, & |x| > 1 \end{cases}$. L3 3 8
- Hence deduce that

$$\int_0^{\infty} \left(\frac{\sin t}{t} \right)^4 dt = \frac{\pi}{3}.$$

14. a i (a) Find $L[t^2 e^{-3t} \sin 2t]$ (b) Find $L\left[\frac{e^{-t} \sin 2t}{t}\right]$. L2 4 8

- ii Using Convolution theorem find the inverse Laplace Transform of $\frac{1}{(s^2+4)^2}$ L3 4 8

Or

- b i Solve $\frac{d^2 y}{dt^2} + 4y = \sin 2t$ where $y(0) = 3$ and $y'(0) = 4$ using Laplace transform. L3 4 8

- ii Find the L.T of the triangular wave function $f(t)$ defined by L2 4 8

$$f(t) = \begin{cases} t, & 0 \leq t < 1 \\ 2 - t, & 1 \leq t < 2 \end{cases} \text{ and } f(t+2) = f(t) \text{ for all } t$$

- | | | | | | | |
|-----|---|----|--|----|---|---|
| 15. | a | i | Find $z^{-1} \left[\frac{10z}{(z-1)(z-2)} \right]$ by using Cauchy's Residue Theorem. | L2 | 5 | 8 |
| | | ii | Find $Z [e^t \sin 2t]$ and $Z [e^{-2t} \sin 3t]$. | L3 | 5 | 8 |
| | | | Or | | | |
| | b | i | Use convolution theorem to evaluate $z^{-1} \left\{ \frac{z^2}{(z-3)(z-4)} \right\}$. | L2 | 5 | 8 |
| | | ii | Solve $y(n+2) + 6y(n+1) + 9y(n) = 2^n$ given $y(0) = y(1) = 0$. | L3 | 5 | 8 |